Biferroic YCrO₃

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YCrO₃, which has a monoclinic structure, shows weak ferromagnetism below 140 K (T_N) and a ferroelectric transition at 473 K accompanied by hysteresis. We have determined the structure and energetics of YCrO₃ with ferromagnetic and antiferromagnetic ordering by means of first-principles density functional theory calculations, based on pseudopotentials and a plane-wave basis. The noncentrosymmetric monoclinic structure is found to be lower in energy than the orthorhombic structure, supporting the biferroic nature of YCrO₃.

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There has been much interest in biferroic materials in recent years.¹⁻⁴ Research in this field is of great interest because of the potential uses of materials with simultaneous ferroelectric and magnetic orderings. Some of these materials exhibit a ferroelectric transition at a relatively high temperature and a magnetic transition at a lower temperature. One such material in this category is BiMnO₃ with the ferroelectric transition (T_E) at 450 K and the ferromagnetic (FM) transition around (T_C) 105 K.^{5,6} BiFeO₃, on the other hand, exhibits a T_E of 1110 K and an antiferromagnetic transition (T_N) at 670 K.⁷ BiCrO₃ is recently reported to exhibit a T_E of 440 K and T_N of 114 K.⁸ Unlike these materials, TbMnO₃ shows a different behavior, wherein T_E is lower than the T_C ; here, the spin frustration causes the ferroelectric distortion. In addition to BiMnO₃, hexagonal rare earth manganates LnMnO₃ (with Ln=Ho, Er, Tm, Yb, Lu, or Y) are known to be biferroic with $T_E \ge T_N$.⁹ Thus, YMnO₃ is ferroelectric around 914 K and antiferromagnetic (AFM) at 80 K.¹⁰ Considering that BiCrO₃, is biferroic just like BiMnO₃, it occurred to us that rare earth chromites such as YCrO₃ may exhibit interesting biferroic properties, a view somewhat strengthened by the suspected ferroelectricity in some of them.11

Careful powder diffraction studies show that YCrO₃ has a monoclinic structure, as reported in the literature,¹² but the Rietveld analysis could not clearly distinguish between the centrosymmetric and noncentrosymmetric structures. However, our first-principles study (discussed later in the paper) has shown the noncentrosymmetric structure to be energetically more stable. YCrO₃ is an antiferromagnet with weak ferromagnetism (T_N =140 K).^{13,14} Our magnetic measurements show an increase in the magnetization around 140 K and the presence of magnetic hysteresis below this temperature (Fig. 1). Clearly, YCrO₃ exhibits features similar to those of a canted antiferromagnetic system.

We have investigated the dielectric properties of pressed pellets as well as thin films of YCrO₃. The thin films were deposited using a KrF excimer laser of 248 nm (lambda physik) at 650 °C in an oxygen ambient of 100 mTorr with pulse energy of 140 mJ/pulse on $\langle 111 \rangle$ oriented Pt/TiO₂/SiO₂/Si substrates. The dielectric phase transition observed in a YCrO₃ pellet is shown in Fig. 2(a). The transition occurs over the 410-440 K range with a maximum (T_{max}) of 418 K at 500 Hz. The T_{max} is frequency dependent. The Curie Weiss plot of $1/\varepsilon$ vs T gives a T_C of 473 K, which is frequency independent as expected of a ferroelectric material.¹⁵ The dielectric constant shows a large dispersion below T_C , but is frequency independent above T_C , a behavior commonly observed in relaxor ferroelectrics.16 The roomtemperature dielectric constant is around 8000 at 5 kHz. A broad transition in normal ferroelectrics is attributed due to the presence of fine grains and the relaxorlike behavior may not be the property of the parent material itself. The presence of charged oxygen vacancies and the short range polar regions can, however, give rise to a relaxorlike behavior in a normal ferroelectric.¹⁷ The role of oxygen vacancies and the presence of nanopolar regions and their role in the relaxorlike behavior in YCrO₃ is under study.

Studies of the YCrO₃ thin films, show a dielectric phase transition around 400 K at 500 Hz as can be seen from Fig. 2(b). The monotonous increase in the dielectric constant at low frequencies above the T_C is associated with the dc conduction. Accordingly, we observe high dissipation factors of 2.348 and 38.834 (5 kHz) at room temperature in the bulk



FIG. 1. Temperature variations of the magnetization of $YCrO_3$ (pellet). The inset shows magnetic hysteresis curves at different temperatures.



FIG. 2. (Color online) Temperature variations of the dielectric constant of $YCrO_3$ (a) pellet and (b) a thin film at different frequencies.

sample and the thin film, respectively. The high-temperature loss shows a monotonous rise due to the increase in the dc leakage current at high temperatures, and efforts are in progress to minimize the losses through processing. The dielectric phase transition found both in the pellets and the thin films also lends evidence for the presence of a ferroelectric phase in YCrO₃.

The ferroelectric behavior of the YCrO₃ pellets and films was also confirmed by their room temperature capacitancevoltage (*C*-*V*) characteristics. The butterfly nature of the *C*-*V* curves [Fig. 3(a)] suggests a weak ferroelectric behavior at room temperature.¹⁸ The room-temperature polarizationelectric field (*P*-*E*) measurements on the pellets and thin films of YCrO₃ show the presence of hysteresis. We show hysteresis curves at different temperatures in Fig. 3(b). The maximum polarization observed is 2 μ C/cm² at 300 K in the case of the pellet and 3 μ C/cm² at 178 K in the case of the thin film. Clearly, YCrO₃ exhibits a weak ferroelectric behavior from *T_E* to low temperatures through the magnetic transition.

Based on measurements of the x-ray powder diffraction data, $P2_1/n$ (space group No. 14) has been suggested as a probable space group for YCrO₃ in the literature.¹² As $P2_1/n$ is a centrosymmetric monoclinic space group, our finding of ferroelectricity in YCrO₃ needs an explanation. To this end, we have carried out first-principles spin-dependent density functional theory calculations using a standard plane-wave code PWSCF 2.0.1 (Ref. 19) with a generalized gradient approximation²⁰ to the interaction energy of electrons. We used ultrasoft pseudopotentials²¹ to represent the interaction between the ions and the electrons and treated semicore *s*



FIG. 3. (a) Capacitance-voltage curves of YCrO₃; (b) dielectric hysteresis in YCrO₃ at different temperatures.

and *p* states of Y and Cr explicitly. An energy cutoff of 30 Ry (180 Ry) on the plane-wave basis was used in representation of wave functions (density). Most calculations involved unit cells with 40 and 20 atoms, and Brillouin zones integrations were sampled with a Monkhorst-Pack mesh of *k* points that is equivalent to a $4 \times 4 \times 4$ uniform mesh²² in the Brillouin zone of a crystal with five atoms per cell. In all calculations, we used experimental lattice parameters or the volume of unit cell.²³

As $P2_1/n$ is a relatively low-symmetry space group, determination of the YCrO₃ structure with many structural parameters becomes challenging. We followed two procedures: (a) We first optimized the structure with a constraint of $P2_1/n$ symmetry. A further relaxation was carried out by breaking its inversion symmetry through off centering of Y and Cr atoms. (b) We started with an initial structure obtained by randomly off centering various atoms in the perovskite unit cell, and relaxed the structure to minimize energy. Structural optimization was first carried out maintaining a G-type antiferromagnetic ordering, and it was reassuring to find essentially the same final structure (Fig. 4) with both the procedures. The final structure has a broken inversion symmetry, supporting the possibility of ferroelectricity in YCrO₃. From the procedure (a), we find that the final AFM structure is indeed lower in energy than the relaxed centrosymmetric $P2_1/n$ phase by 0.025 eV/formula unit. Our guess for the space group of the lowest energy structure of YCrO₃ is the monoclinic $P2_1$ (No. 4), though we find tiny distortions of the structure that amount to further lowering of symmetry. In this distorted perovskite structure, the average oxygen coor-



FIG. 4. (Color online) Structure of AFM YCrO₃ (8 formula units/cell): (a) structural distortions of the parent centrosymmetric structure are shown with arrows with lengths proportional to atomic displacements from the cubic structure, (b) cubelike surfaces surrounding Cr atoms are the isosurfaces of magnetization density at a value 10% of its maximum. We have used XCRYSDEN software for visualization (Ref. 26).

dination of Y is about 6. Structural distortions of the parent cubic perovskite structure leading to the ferroelectric structure [shown in Fig. 4(a)] have been analyzed by writing them as a linear combination of normal modes of the cubic structure. For YCrO₃, we find the largest component of structural distortions to be associated with (a) M_3 modes $[k=(011) \pi/a]$, (b) R_{25} modes $[k=(111) \pi/a]$, which correspond to rotations of oxygen octahedral, and (c) M_5 modes. There is a small component of modes with Y and oxygen displacements such as X_5' , R_{15} , and Γ_{15} modes. There are no structural distortions with Cr displacements. The modes in (a) and (b) dominating the low-temperature phase do not break the inversion symmetry, while the relatively weak distortions of the mode Γ_{15} give rise to ferroelectricity.

Using the relaxed structure with AFM ordering as an initial guess, we optimized the structure of $YCrO_3$ with ferromagnetic ordering. While the relaxed structure with ferro-



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FIG. 5. Density of electronic states with spin up (positive) and down (negative) near the energy gap of monoclinic structures with (a) antiferromagnetic and (b) ferromagnetic ordering.

magnetic ordering also exhibits a broken inversion symmetry, it is higher in energy than the structure with *G*-AFM ordering by about 0.04 eV/formula unit. For both types of ordering, the self-consistently determined local magnetic moment at the Cr site is close to 3 μ_B consistent with fully occupied t_{2g} states of Cr just below the energy gap, as seen in the densities of electronic states (shown in Fig. 5). This results in a spin density with almost cubic symmetry centered at the Cr sites [see Fig. 4(b)]. Unlike many other materials, YCrO₃ is insulating in both FM- and AFMordered states with an energy gap of 1.3 and 1.8 eV, respectively, and exhibits a large exchange splitting. We used the Berry phase²⁴ method to compute polarization and find *P* along the *a* axis to be about 3 μ C/cm².

To understand the origin of ferroelectricity in YCrO₃ we studied the structural instabilities in the cubic perovskite structure of YCrO₃. We used a unit cell doubled along the $\langle 111 \rangle$ direction with a *G*-type AFM ordering and determined phonon frequencies at its Γ point, which correspond to phonons at Γ and *R* (folded for the supercell) points of the

single perovskite unit cell. We find two triply degenerate instabilities, the strongest one (about 300 cm⁻¹) exhibits rotational motion of oxygen octahedra, and a weaker instability (about 100 cm⁻¹) of Y displacements with respect to oxygen cage. Note that the former gives an antiferrodistortive phase while the latter is responsible for a ferroelectric phase. To probe anharmonic strength of the ferroelectric instability, we distorted the structure by freezing in Y displacements and relaxed it maintaining a rhombohedral symmetry and G-AFM ordering. We find an energy lowering by 0.089 eV/formula unit, comparable to other perovskite ferroelectrics like PbTiO₃.²⁵ Interestingly, for a rhombohedral symmetry and FM ordering, optimized ferroelectric structure is lower than the paraelectric structure by 0.13 eV/formula unit, though is higher in energy than the ferroelectric structure with AFM ordering. In both FM and AFM ordering, the off centering of Cr atoms is not favored energetically.

In conclusion, our experimental results clearly demonstrate YCrO₃ to be biferroic, with interesting magnetic properties. Our calculations support the observed ferroelectricity in YCrO₃ through the determination of the detailed structure. There are competing structural instabilities in YCrO₃, and

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the dominating one is of antiferrodistortive type. Hence, the polarization found in YCrO₃ arising from the weak ferroelectric instability is relatively small. Our finding that the G-type AFM ordering is lower in energy than the uniform FM ordering is consistent with the experimentally known AFM phase of YCrO₃ and indicates that ferromagnetism in YCrO₃ can only be weak and its emergence at lower temperatures must be from mechanisms other than simple exchange-type magnetic interactions, possibly canted AFM. It is possible that noncentrosymmetry in YCrO₃ is local in nature, an aspect that can be revealed by a study of the pairdistribution functions based on careful diffraction measurements. It appears likely that other chromites of heavier rare earths (Er, Ho, Yb, Lu) may also be biferroic. Our preliminary measurements show that LuCrO₃ becomes ferromagnetic at 115 K (T_N) and ferroelectric at 488 K (T_E) . Further studies are in progress on these chromites.

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