First-Principles Study of One-dimensional Nano-structures

 $\begin{array}{c} \text{A Thesis} \\ \text{Submitted For the Degree of} \\ \\ DOCTOR \ OF \ PHILOSOPHY \end{array}$

by Mousumi Upadhyay Kahaly



THEORETICAL SCIENCES UNIT

JAWAHARLAL NEHRU CENTRE FOR ADVANCED SCIENTIFIC

RESEARCH

Bangalore - 560 064

(A Deemed University)

AUGUST 2007

To my parents

DECLARATION

I hereby declare that the matter embodied in the thesis entitled "First-Principles Study of One-dimensional Nano-structures" is the result of investigations carried out by me at the Theoretical Sciences Unit, Jawaharlal Nehru Centre for Advanced Scientific Research, Bangalore, India under the supervision of Prof. Umesh V. Waghmare and that it has not been submitted elsewhere for the award of any degree or diploma.

In keeping with the general practice in reporting scientific observations, due acknowledgement has been made whenever the work described is based on the findings of other investigators.

Mousumi Upadhyay Kahaly

CERTIFICATE

I hereby certify that the matter embodied in this thesis entitled "First-Principles Study of One-dimensional Nano-structures" has been carried out by Ms. Mousumi Upadhyay Kahaly at the Theoretical Sciences Unit, Jawaharlal Nehru Centre for Advanced Scientific Research, Bangalore, India under my supervision and that it has not been submitted elsewhere for the award of any degree or diploma.

Prof. Umesh V. Waghmare (Research Supervisor)

Acknowledgements

At the moment of this thesis submission, I have two reasons to celebrate: firstly, I see my dream of becoming a doctorate coming to fruition very soon, and secondly, I inched one step closer to being what I always wanted to be, a scientist. Its seems apparently paradoxical that at this juncture, instead of remembering all the moments that truly gave me immense satisfaction as a student of science, I feel very emotional, remembering them on whose shoulders I built my ph.D. First among them is undoubtedly, my research supervisor, Prof. Umesh V. Waghmare. He has been an epitome of excellence, patience and kindheartedness. His sheer enthusiasm for science, drive for perfection and elan in pointing out the basics have always amazed me. He taught me how to understand a problem in terms of mathematics and search for concrete solutions. I am and will remain deeply indebted to Umesh sir, whose help, stimulating suggestions and encouragement to be independent helped me during the time of research and which I would carry forward rest of my life. But, for his inputs, teachings and support, this thesis would not have shaped up.

I wish to express my gratitudes to Prof. Shobhana Narasimhan. She has been an outstanding teacher; not only teaching solid state physics, she taught me the art of being self-critical and communicative with clarity in expressions. Through these 5 years I have benefited immensely by interactions with the professors in JNCASR: Prof. Swapan Pati, Prof. Srikanth Sastry, Prof. Chandrabhas Narayana, Prof. Sundaram Balasubramanian, Prof. Rama Govindarajan, Prof. G. U. Kulkarni, Dr. N. S. Vidhyadhiraja and learnt lots from them.

Many thanks to Prof. M. R. S. Rao and Prof. C. N. R. Rao for their

part in creating a beautiful academic environment and the numerous scientific facilities that JNCASR boasts today. Prof. C. N. R. Rao's works on selenium and tellurium nanowires were the major motivating factors behind the projects I describe in Chapter 4. His passion for science and acumen to pursue it have had a permanent effect on me and my love to science.

Chapter 3 of this thesis was motivated by the experiments by our collaborators, Prof. Murali Sastry, Prof. B. L. V. Prasad and Dr. Tanushree bala from NCL, Pune; I take this opportunity to thank them.

Thanks are due to my friends in JNCASR, IISC, TSU friends and specially my lab mates for being source of support in time of need. I specially thank Gargi didi, Tiju, Aditi, Prasenjit and Aarti for all their support which went beyond academics. I feel blessed to have got their company.

There were moments, when I went weaker in confidence as things went tougher. My school, college and university teachers who had faith in me and believed that I would "do well", have all been my pillars of strength.

My family, all my relatives have been with me throughout. It was their support and encouragement that helped me to pursue what I wanted, a research career. That way, what I am today, professionally and personally, is because of them. Two years into my PhD I got married to Subhendu, a research scholar like me at the TIFR. Its an understatement to say that he was my best friend through these years. He has been more than that....its rightly said: "some things are better left unsaid". My parents, my brother and sister are the greatest gifts that I have ever received from God. My in-laws, were never less than my parents. I know for sure that they all are with me, in every way they possibly can, just to make my life beautiful. My grandma, uncles, aunts have always been extremely supportive and indulgent. I accept my failure to thank them enough here.

I am thankful to Mr. Jayachandra, Dr. Subbarao, Dr. Kavitha Sridhar, Sukanya madam and Princy madam, JNC computer lab administrators for all their help. I beg pardon if I have left out any name from the list. But, I wish to just express my heartfelt thanks to all the people who filled my life with light and happiness and dream.

Synopsis

For the last fifteen years, the field of nanomaterials has been an active area in scientific research due to the enormous promise of nanosystems for prospective applications in areas like nano-electronics, nano-mechanics, and medical instrumentation etc. This doctoral thesis is aimed at gaining a theoretical understanding of the physical and chemical properties of one dimensional nanostructures, and use this understanding for novel applications. Most of this work is performed within the framework of first-principles density functional theory.

In the first project, we study interaction of inorganic metal ions (M) with organic molecules like acetic acid, resulting in the formation of metal diacetates and attempt to understand the diversity in geometry and properties of binding of different metal ions with -COOH group. The estimates of metal-acetate bond energies follow trends found experimentally, and can be used for selective removal of metal ions, i.e. in ion sensor.

The second project determines the size-dependence of atomic and electronic structures, elastic properties and most importantly, optical conductivity of selenium nanowires. Though the interchain bonding between two helical chains in trigonal selenium based nanowires is weak enough to have only a small impact on structure, the features in the optical conductivity obtained from the electronic structure show marked anisotropy and interesting dependence on the diameter of a Se nanowire. Our results raise the possibility that bundles of aligned Se nanowires can be used as nano-polarizers. Further, the origin of stability of the helical structure of selenium is investigated through Wannier functions based study of chemical bonding in Se nanowires and clusters.

In the third project we estimate and understand effects of curvature on structures and vibrations of armchair and zigzag carbon nanotubes. An understanding of the effect of curvature on phonon dispersion of nanotubes is developed through its correlation with the normal modes of an unrolled graphene sheet. Within a quasiharmonic approximation, we estimate thermal expansion coefficient of carbon nanotubes and identify the low energy vibrational modes that dominate their negative thermal expansion at low temperatures. Further, we study size-dependence of thermal properties of carbon nanotubes to find that while the specific heat is found to depend rather weakly on the diameter of nanotubes, their negative thermal expansion behavior exhibits a relatively stronger dependence on the diameter. Study of full phonon dispersion and thermal properties in double wall carbon nanotubes illustrates the effect on inter-tube interaction on their negative thermal expansion at low temperatures.

In the fourth project, we determine atomic and electronic structures of arm-chair and zigzag boron nitride nanotubes of different diameters, and understand the effect of doping in such nanotubes. We find that carbon substitution either at B-site, or at N-site in a pristine boron nitride nanotube yields magnetically polarized semiconducting state, whereas carbon substitution at neighbouring B and N sites yields a non-magnetic insulating structure. In contrast to the above spontaneous magnetization, B or N doping in carbon nanotubes gives a simple shift in the Fermi energy and maintains a non-magnetic state. Thus, C-doped boron nitride nanotubes opens up the possibility of getting metal-free magnetic semiconducting nanotubes which can be used as memory device or nano-manipulator.

Finally, in our fifth project, we propose novel types of nano-tubes, such as carbon nanotubes with fractional indices of helicity These carbon based nano-structures of considerable stabilities open up possibilities of design of novel nano-composites, nano-electronic interconnects etc. For example, the class of carbon nano-tubes based on stacking faults in graphene sheet exhibit unusual electronic structure with carrier states confined truly within one dimensional space.

In summary, this thesis is a first-principles theoretical investigation of

different one dimensional nano-structures and related systems, with emphasis on both their fundamental and applied aspects.

Nomenclature

0D: zero-dimensional

1D: one-dimensional

2D: two-dimensional

3D: three-dimensional

e: charge of an electron

BE: binding energy

BFGS: Broyden, Fletcher, Goldfarb, Shannon

BO: Born and Oppenheimer

DFT: density funtional theory

DFPT: density functional perturbation theory

DOF : degrees of freedom

DOS: density of states

HK: Hohenberg and Kohn

GGA: feneralized gradient approximation

LDA: local density approximation

PBE : Perdew, Burke and Ernzerhof exchange-correlation functional

PW91: Perdew and Wang exchange-correlation functional

 m_e : mass of an electron

 M_I : mass of nuclei

Se-h: a single Se helix

Se-w1: Se wire with one shell

Se-w2: Se wire with two shells

 α, β : Cartesian indices

a: lattice spacing

A: area

 d_b : bond length

E: total energy of a system

 E_{cut} : Plane wave energy cut-off

 E_{e-e} : electron-electron interaction energy

 $E_n(\mathbf{R})$: BO potential energy surface

 $E_{tot}[n]$: Total energy functional

 E_{Ewald} : nuclear-nuclear interaction for a particular ionic configuration

 E_{HK} : HK functional

 $E_{\rm XC}[n]$: exchange-correlation energy

 $E_{\rm XC}^{\rm LDA}$: exchange-correlation energy within the LDA

 $E_{\mathrm{XC}}^{\mathrm{GGA}}$: exchange-correlation energy within the GGA

h: Planck's constant

 \hbar : $h/2\pi$

 \hat{H} : Hamiltonian

 \mathbf{k} : wave vector

 k_B : Boltzmann constant

 μ_B : Bohr magneton

 ∇ : spatial derivative

 $n(\mathbf{r})$: electronic charge density

 $n_0(\mathbf{r})$: ground state electronic charge density

N: number of electrons

 ω : frequency

 Ω : volume of the unit cell

 r_c : cut-off radius

 \mathbf{r}_i : position of $i^{ ext{th}}$ electron

 \mathbf{R}_I : position of $I^{ ext{th}}$ ion

R: radius of nanowire

 σ : conductivity tensor

 θ : bond angle

T: temperature

T[n]: kinetic energy functional

 $T_0[n]$: ground state kinetic energy functional

 v_{XC} : functional derivative of the exchange-correlation energy

 $v_{\rm XC}^{\rm LDA}$: exchange-correlation potential within LDA

 $v_{\mathrm{XC}}^{\mathrm{GGA}}$: exchange-correlation energy within the GGA

 $V_{
m ext}({f r})$: external potential

V: volume

 V_0 : volume of nanowires

Y: Young's modulus

 Z_I : charge of nuclei

 Z_I : charge of nuclei

CNT: carbon nanotubes

SWCNT: single walled carbon nanotubes

 α : thermal expansion coefficient

 C_p : specific heat

GP: Gruneisen parameter

NTE: negative thermal expansion

Contents

A	ckno	wledge	ements	\mathbf{v}
Sy	ynops	sis		vii
N	omei	ıclatur	r e	x
1	Inti	oducti	ion	1
	1.1	Histor	y and current status of science and technology of nanos-	
		tructu	res	. 1
	1.2	Nanos	tructures: between atoms and condensed matter	. 3
	1.3	One d	imensional nanostructures	. 4
	1.4	Tools	for handling nanostructures	. 5
	1.5	First-1	principles calculations: why and what?	. 7
	1.6	Summ	ary of the systems studied in the thesis	. 8
		1.6.1	Motivations	. 8
	1.7	Future	e Prospects of "nano"	. 10
2	Cor	nputat	ional methods	11
		2.0.1	Born-Oppenheimer approximation	. 12
	2.1	Densit	sy Functional Theory	. 13
		2.1.1	Hohenberg-Kohn formalism	. 13
		2.1.2	The Kohn-Sham equations	. 14
		2.1.3	Exchange and correlation	. 15
		2.1.4	Calculation of Total Energy	. 18
		2.1.5	Basis set	. 18

		2.1.6 Pseudopotentials	20
		2.1.7 k-point sampling and smearing of occupation numbers	22
		2.1.8 Calculation of Forces and Stresses	23
	2.2	Calculation of phonons	24
		2.2.1 Frozen phonon method	25
		2.2.2 Density functional perturbation theory	26
	2.3	DFT codes usd in this thesis	28
3	$\operatorname{Int}\epsilon$	eraction of different metal ions with carboxylic acid group:	
	Αq	quantitative study	30
	3.1	Introduction	30
	3.2	Experimental background and Motivation	32
	3.3	Computational Details	33
	3.4	Results and discussion	34
		3.4.1 Energetics and structures of metal diacetates	36
		3.4.2 Charge density analysis	41
		3.4.3 Stiffness of M-A binding	43
	3.5	Conclusions	45
4	Size	e dependence of structural, electronic, elastic and optical	·
	pro	perties of selenium nanowires	51
	4.1	Introduction	51
	4.2	Methods	53
	4.3	Results for bulk Se	54
	4.4	Structures and elastic properties for Se-h, Se-w1, Se-w2 and	
		bulk Se	57
		4.4.1 A comparative study of structures	58
		4.4.2 Elastic properties of Se-h, Se-w1 and Se bulk	60
	4.5	Electronic Structure	64
		4.5.1 Se-h	65
		4.5.2 Se-w1	65
		4.5.3 Se-w2	66
		4.5.4 Bulk Se	67

	4.6	Optical conductivity	69
	4.7	The origin of stability of helical structure: Se clusters	73
		4.7.1 Clusters: energetics and stability	74
		4.7.2 Stability of helical structure, in light of bonding orbitals	75
	4.8	Summary and Discussion	77
5	Effe	ect of curvature on structures and vibrational properties	
	of c	arbon nanotubes	86
	5.1	Introduction	86
	5.2	Methods	88
		5.2.1 Benchmarking our method for two allotropes of carbon:	
		diamond and graphite	89
	5.3	Structural and electronic properties of SWCNTs in isolated	
		and bundled forms	90
	5.4	Stability and electronic structures of double wall carbon nan-	
		otubes	95
	5.5	Effect of curvature on vibrations of CNT	96
		5.5.1 Phonon dispersion of DWNT (8,8)(13,13)	99
	5.6	Summary	100
6	Size	e-dependence of thermal properties of carbon nanotubes1	.09
	6.1	Introduction	109
	6.2	Methods	110
	6.3	Specific and thermal expansion of CNTs	111
	6.4	Summary	117
7	Effe	ect of doping: Contrast in the electronic and magnetic	
	pro	perties of doped carbon and boron nitride nanotubes 1	18
	7.1	Introduction	118
	7.2	Methods	120
		7.2.1 Technical Details	
		7.2.2 Structures of graphite, boron nitride and their single	
		layer forms	121
	7.3	Properties of SWBN-NTs in isolated and bundled forms	193

		7.3.1	Geometry
		7.3.2	Stability and atomic structures
		7.3.3	Electronic structures of pristine BN-NTs
	7.4	Doped	CNT and BN-NT
		7.4.1	Energetics of doped CNTs and doped BN-NTs 128
		7.4.2	Effect of boron or nitrogen doping on the electronic properties of CNT
		7.4.3	Effect of carbon doping on the electronic properties of
		D	BN-NT
	7.5	Discuss	sion and Summary
_	~	•	
8	Sen	11-meta	llic carbon nanotubes with fractional indices of
8		11-meta ality	llic carbon nanotubes with fractional indices of 147
8		ality	
8	chir	ality Metho	147
8	chir 8.1	r ality Method Introdu	147 ds
8	chir 8.1 8.2	r ality Method Introdu	147 ds
8	chir 8.1 8.2	eality Method Introdu CNTs	147 ds
8	chir 8.1 8.2	Method Introdu CNTs 8.3.1 8.3.2	147 ds
8	chir8.18.28.3	Method Introdu CNTs 8.3.1 8.3.2 Phonor	147 ds
8	chir 8.1 8.2 8.3	Method Introdu CNTs 8.3.1 8.3.2 Phonor	ds .